Roll No.
Total No. of Pages: 03
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## B.Tech All (Sem. - 2)

## MATHEMATICS-II

Subject Code: BTAM- 204-18
M Code: 76257
Date of Examination : 23-01-23
Time: 3 Hrs.
Max. Marks: 60

## INSTRUCTIONS TO CANDIDATES:

1. SECTION-A is COMPULSORY consisting of TEN questions carrying TWO marks each.
2. SECTION - B \& C have FOUR questions each, carrying EIGHT marks each.
3. Students have to attempt any FIVE questions from SECTION B \& C, selecting atleast TWO questions from each of these SECTIONS B \& C.

## SECTION-A

1. Answer the follwoing:
a) Name any four measures of dispersion.
b) Define kurtosis.
c) Two cards are drawn at andom from a well-shuffled pack of 52 cards. What is the probability of drawing twaces?
d) Give the formulactifnean and standard deviation for Poisson distribution.
e) Write any foc properties of normal distribution.
f) Find the coefficient of correlation of two independent variables $x$ and $y$.
g) Write the normal equations for the curve $x=b+c y$.
h) Define standard error of mean and level of significance.
i) Define Type-II error.
j) Define null hypothesis.

## SECTION-B

2. a) Calculate standard deviation from the table giving marks distribution of 112 students:

| Marks | $20-30$ | $30-40$ | $40-50$ | $50-60$ | $60-70$ | $70-80$ | $80-90$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of students | 5 | 14 | 24 | 27 | 18 | 15 | 9 |

b) The first four moments of distribution about the value 5 of the variable are $2,20,40$ and 50 . Obtain the moments about mean.
3. a) Two unbiased dice are thrown. Find the expected values of the sum of numbers of points on them.
b) A and B take turns in throwing two dice, the first to throw 10 being awarded the prize. If A starts first, find their chances of winning.
4. a) A man tosses a fair coin 10 times. Find the probability that he will have:
i) Not more than 5 heads
ii) A minimum of 4 heads
b) A manufacturer of cotter pins knows that $5 \%$ of his product is defective. If he sells cotter pins in boxes of 100 and guarantees that not more than 10 pins will be defective, what is the approximate probability that a box will fail to meet the guaranteed quality?
5. a) If $X$ is normally distributed and the mean of $X$ is 30 and the standard deviation is 5 . Find out the probability of the following:
i) $X \geq 45$
ii) $26 \leq X \leq 40$
b) Marks obtained by 10 students in Mathematics and Statistics are given below. Find the coefficient of correlation between the two subjects.

| Mathematics | 30 | 60 | 80 | 53 | 35 | 15 | 40 | 38 | 48 |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Statistics | 85 | 45 | 54 | 91 | 58 | 63 | 35 | 43 | 45 | 44 |

## SECTION-C

6. A continuous random variable $X$ has a probability density function $f(x)=3 x^{2}, 0 \leq x \leq 1$. Find $a$ and $b$ such that
i) $P\{X \leq a)=P\{X>a\}$
ii) $P\{X>b\}=0.05$
7. Fit a parabola of second degree to the data:

| Time (sec) | 1 | 2 | 3 | 4 | 5 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Distance (feet) | 15 | 70 | 140 | 250 | 380 |

8. a) The mean produce of wheat of a sample of 100 fields is 200 kg per acre with a standard deviation of 10 kg . Another sample of 150 fields has the mean at 220 kg with a standard
deviation of 12 kg . Assuming the standard deviation of the yield at 11 kg , find out if there is a significant difference between the mean yields of the two samples.
b) A random sample of 500 pineapples was taken from a large consignment and 65 were found to be bad. Find the standard error of the proportion of bad ones in a sample.
9. a) Test whether the colour of the son's eyes is associated with that of the father's as per the data given below:

|  |  | Eye colour of sons |  |
| :---: | :---: | :---: | :---: |
|  |  | Black | Brown |
| Eye colour of fathers | Black | 2 | 10 |
|  | Brown | 6 | 6 |

(Take $\chi_{0.05}^{2}$ for 1 degree of freedom $=3.841$ )
b) The mean height of 50 male students who participate in college athletics was 68.2 inches with a standard deviation of 2.5 inches; while 50 male students who do not participate in athletics had a mean height of 67.5 inches with a standard deviation of 2.8 inches. Test the hypothesis that male students who participate in college athletics are taller than other male students.

NOTE : Disclosure of Identity by writing Mobile No. or Marking of passing request on any
paper of Answer Sheet will lead to UMC against the Student.

