Roll No.						

Total No. of Pages: 02

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#### B.Tech (Sem. - 1)

## MATHEMATICS-I

#### Subject Code: BTAM-101-18

#### M Code: 75353

#### Date of Examination : 11-01-2023

Time: 3 Hrs.

Max. Marks: 60

INSTRUCTIONS TO CANDIDATES:

- 1. SECTION-A is COMPULSORY consisting of TEN questions carrying TWO marks each.
- 2. SECTION B & C have FOUR questions each, carrying EIGHT marks each:
- 3. Attempt any FIVE questions from SECTION B & C, selecting atleast TWO questions from each of these SECTIONS B & C.

## SECTION-A

- 1. Answer the following:
  - a) Give geometric interpretation of mean value theorem.
  - b) Can Rolle's theorem be appled to the function:
    - $f(x) = \begin{cases} x, & 0 \leq x \leq 1 \\ 2-x, & 1 \leq x \leq 2 \end{cases}$  in the interval  $[0, \pi]$ .
  - c) Evaluate  $\lim_{x \to 0} [x^n (\ln x)]$ .

d) Does the limit 
$$\lim_{(x,y)\to(0,0)} \frac{xy}{x^2+y^2}$$
 exists?

- e) Give the coordinates of the center of gravity of solid of mass *M*.
- f) Define convergence, divergence and oscillation of a series.
- g) Define D'Alembert's ratio test to check the convergence of the positive term series  $\sum u_n$ .
- h) Find sum and product of Eigen values of the matrix  $\begin{bmatrix} 1 & -1 \\ 2 & -5 \end{bmatrix}$ .
- i) Find the inverse of the matrix  $\begin{bmatrix} 3 & 1 \\ 1 & 4 \end{bmatrix}$ .
- j) Find rank of the matrix  $\begin{bmatrix} 0 & 1 & -3 \\ 1 & 0 & 1 \\ 3 & 1 & 0 \end{bmatrix}$ .

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#### **SECTION-B**

- 2. a) Expand  $f(x) = e^x$  in powers of (x 1) upto four terms.
  - b) Evaluate the limit  $\lim_{x \to 0} \frac{e^{x} e^{-x} 2\log(1+x)}{x \sin x}$
- 3. a) Find the volume of the loop generated by the revolving the curve  $y^2(a + x) = x^2(3a x)$ about the x axis.
  - b) Find extremum of the function  $2\sin x + \cos 2x$ ,  $0 \le x \le 2\pi$ .
- 4. a) Discuss the continuity of the function  $f(x, y) = \begin{cases} \frac{x^2 + y^2}{xy}, (x, y) \neq (0, 0) \\ 0, (x, y) = (0, 0) \end{cases}$  at (0, 0).
  - b) Find extreme values of 2x + 3y + z subject to the conditions x + z = 1 and  $x^2 + y^2 = 5$ .
- 5. a) Evaluate the integral  $\iint_R e^{x^2} dx dy$ , where R is the region given by  $R: 2y \le x \le 2 \text{ and } 0 \le y \le 1$ 
  - b) Evaluate  $\iiint_T (x + 3y 2z) dx dy dz$ , over the boundary of  $T: 0 \le y \le x^2, 0 \le z \le x + 1$  $v, 0 \leq x \leq 1$ .

- 6. Examine the convergence of the series  $\sum \frac{3 \cdot 6 \cdot 9 \cdots (3n)}{7 \cdot 10 \cdot 13 \cdots (3n+4)} x^n$ .
- 7. a) Examine the convergence of the series  $\frac{1}{1,2,3} + \frac{1}{2,3,4} + \frac{1}{3,4,5} + \cdots$ 
  - b) Examine the convergence of the alternating series  $1 \frac{1}{2^k} + \frac{1}{3^k} \frac{1}{4^k} + \cdots$ , for k > 0.
- 8. Find the characteristic equation of the matrix  $\begin{bmatrix} 1 & 4 \\ 2 & 3 \end{bmatrix}$  and hence compute  $A^{-1}$ . Find the matrix represented by  $A^5 4A^4 7A^3 + 11A^2 A 10I$ .
- 9. Reduce the matrix  $\begin{bmatrix} 5 & 3 & 7 \\ 3 & 26 & 2 \\ 7 & 2 & 10 \end{bmatrix}$  to the diagonal form.

**NOTE : Disclosure of Identity by writing Mobile No. or Marking of passing request on any** paper of Answer Sheet will lead to UMC against the Student.

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