Paper Id: $\square$ Roll No. $\square$

## B TECH

(SEM-IV) THEORY EXAMINATION, 2018-2019
MATHEMATICS-III
Time: 3 Hours
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1. Attempltquestiontsrief.
a. Write the statement of Cauchy's Integral formula
b. Find the residue at the pole of the function $(z)=\frac{z^{3}}{(z-2)^{\text {m }}}$
c. Write the normal equations of the curve $=a+\frac{b}{x^{m}}+\frac{c}{x^{య}}$
d. A die is tossed thrice .A success is getting 4 or 5 on a toss.Find the mean and variance of the number of successes.
e. Show that $\mu^{2}=1+\frac{1}{4} \delta^{2}$.
f. Using Euler's method solves the differential equation in three steps: $\frac{d y}{d x}=x+$ $y^{2}, y(1)=2$ and $h=0.2$.
g. Find the Z-transform of $\{-2,-1,0,2,4,5,10,15\}$.

## SECTION B

2. Attempt any three of the following:
$7 \times 3=21$
a. State and prove Taylor's theorem.
b. Solve the following system by Jacobi's method:

$$
\begin{gathered}
x+y+54 z=110 \\
27 x+6 y-z=85 \\
6 x+15 y+2 z=72
\end{gathered}
$$

c. Find the root of the equation $x e^{x}=\cos x$ by the Regula Falsi method, up to four decimal places.
d. Out of 1000 families wh four children each, how many families would be expected to have: (i) 2 boys and 60 irls; (ii) at least one boy;(iii)no girl (iv) at most two girls ?
e. $\quad$ Solve the differface equation $y_{k+3}-3 y_{k+2}+3 y_{k+1}-y_{k}=U(k)$ where $y_{0}=y_{1}=$ $y_{2}=0$ by using, 2 -transform.

## SECTION C

3. Attempt any $q$, part of the following:
(a) Prove that $u=x^{2}-y^{2}-2 x y-2 x+3 y$ is harmonic. Find a function $v$ such that $f(z)=u+i v$ is analytic .Also express $f(z)$ in terms of $z$.
(b) Expand $f(z)=\frac{1}{z^{4} 3 z+2}$ in the region (i) $|z|<1$ (ii) $1<|z|<2(i i i)|z|>2$
4. Attempt any one part of the following:

$$
7 \times 1=7
$$

(a) The following regression equations and variances are as follows: $0,5 y-4 x-3=0$, variance of $x=9$. Find the value of (i )mean values of $x$ and $y$ (ii )the coefficient of correlation between $x$ and $y$,(iii) the standard deviation of $y$.
(b) Fit a curve $y=a e^{b x}$ to the following data:

| x | 1 | 2 | 3 | 4 | 5 | 6 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| y | 7.209 | 5.265 | 3.846 | 2.809 | 2.052 | 1.499 |

5. Attempt any one part of the following:
$7 \times 1=7$
(a)

| Find missing term, given that |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| X 0 5 10 15 20 <br> 25      <br> Y 6 10 $\cdots$ 17 $\cdots$ <br> 31      |  |  |  |  |  |  |

(b) Find the values of $\mathrm{F}(2), \mathrm{F}(8)$ and $\mathrm{F}(15)$ from the following table:

| $x$ | 4 | 5 | 7 | 10 | 11 | 13 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{~F}(\mathrm{x})$ | 48 | 100 | 294 | 900 | 1210 | 2028 |

6. Attempt any one part of the following:
(a) Use the Runge - Kutta method of fourth order to find $\mathrm{y}(0.1)$ with $\mathrm{h}=0.05 \frac{d y}{d x} \mathrm{r}=$ $\sqrt{x+y}$, where $y(0)=1$.
(b) State and prove Trapezoidal rule for numerical integration.
7. Attempt any one part of the following:
(a) Find the Fourier sine transform of $F(x)=\frac{e^{a \circ} \times \mathrm{ms}}{x}$.Hence find the Fourier sine transform of $(x)=\frac{1}{x}$.
(b) Find $Z^{-1}\left(\frac{z^{\text {M }}}{(z-5)(z-6)^{\text {a }}}\right)$.
