

Roll No.....

8411

Printed Pages : 4

BT-4/M-14

SIGNAL AND SYSTEMS

Paper-EE-208-E

Time allowed : 3 hours]

[Maximum marks : 100

Note : Attempt five questions in all, selecting at least one question from each section.

Section-1

1. (a) Explain even and odd signals with examples. Find the even and odd components of the signal :

$$x(t) = 7t^3 + 5t^2 + 2t + 4. \quad 5$$

- (b) Find the Fourier transform of a unit step function. 5

- (c) Explain the time-shifting and frequency shifting property of Fourier transform. 10

2. (a) State the Convolution theorem and give its significance.

Prove the following properties of convolution :

- (i) Distributive property, and
- (ii) Associative property. 10

- (b) (i) Explain the Dirichlet conditions for convergence of Fourier transform. 5

- (ii) Determine the Laplace transform of $t \sin t$. 5

(2)

Section-2

3. (a) State and prove sampling theorem. 10

- (b) What is discrete time decimation and interpolation ? What is its significance ? Mathematically show the effect of decimation and interpolation in the frequency domain. 10

4. (a) What is PDF ? How do we get PDF from probability distribution function ? 10

- (b) Find the inverse z-transform of

$$x(z) = \frac{1 - z^{-1} + z^{-2}}{(1 - \frac{1}{2}z^{-1})(1 - 2z^{-1})(1 - z^{-1})}$$

with ROC $1 < |z| < 2$. 10

Section-3

5. (a) What do you mean by causal and non causal system and lines and non linear system ? Given a continuous time system with input $x(t)$ and output $y(t)$ related by $y(t) = x(\sin(t))$. Find the following :

- (i) Is this system causal ?
- (ii) Is this system linear ? 10

(3)

8411

- (b) Write a note on the following :
- SISO
 - MISO.
6. (a) For the following input output relationships, determine whether the corresponding system is linear, time invariant or both ?
- $y(t) = t^2 x(t-1)$
 - $y[n] = x^2[n-2]$
- (b) Determine whether the system described by $y(t) = \cos(x(t))$ is :
- Memoryless
 - Stable
 - Causal
 - Linear
 - Time invariant.

Section-4

7. (a) What do you mean by transfer function ? 5
- (b) What are the advantage of using state variable technique for system modelling ? 5
- (c) Consider a stable LTI system that is characterised by differential equation :
- $$\frac{d^2}{dt^2} y(t) + 4 \frac{d}{dt} y(t) + 3y(t) = \frac{d}{dt} x(t) + 2x(t).$$
- Find the impulse response of the system. 10

8411

P.T.O.

(4)

8. (a) State and prove the causality and stability property of LTI system. 10
- (b) Define transfer function. Find the transfer function of the system described by the following differential equation :
- $$\frac{d^2}{dt^2} y(t) + 11 \frac{d}{dt} y(t) + 24y(t) = \frac{5d}{dt} x(t) + 3x(t)$$
- with zero initial conditions. 10

8411