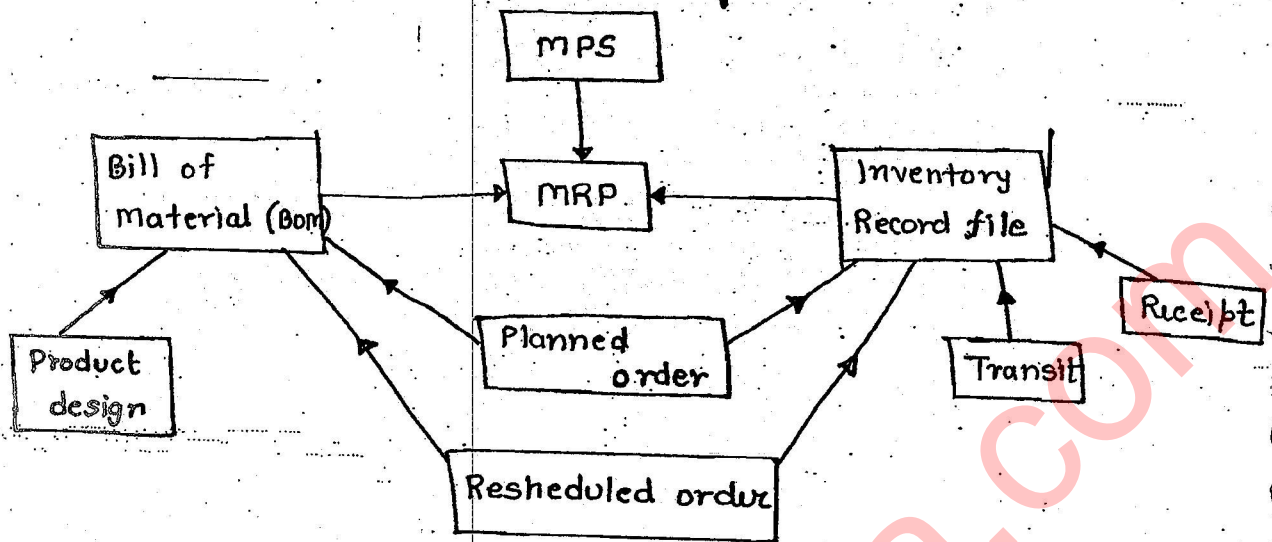


MATERIAL REQUIREMENT PLANNING (MRP)



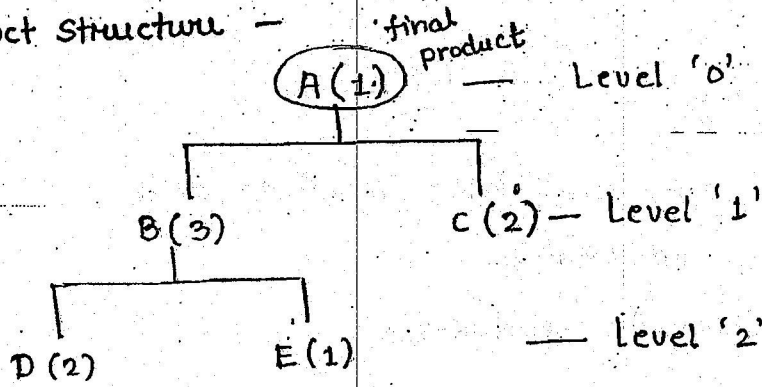
MRP is a method of working out the production plan in a multi stage production system that produces many product and require raw material and sub assembly. It is used to show that all the things needed should be available within the production system at an appropriate time and production can be carried out without any delay. Today MRP is a computer based information system for production, scheduling and purchasing of dependant demand item.

Master Production Schedule (MPS) is a complete time table of our scheduled prodⁿ in future. It gives information about which product is to be produced, when it is to be produced and in what quantity.

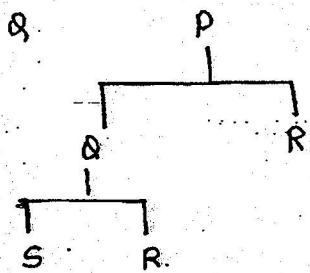
Inventory Record File :- This file gives complete and upto date information about on hand inventory, transit inventory, scheduled receipt and planned order.

Bill of Material gives information about how each final product is manufactured specifying all sub-component and their sequence of build-up in their final product.

product structure -



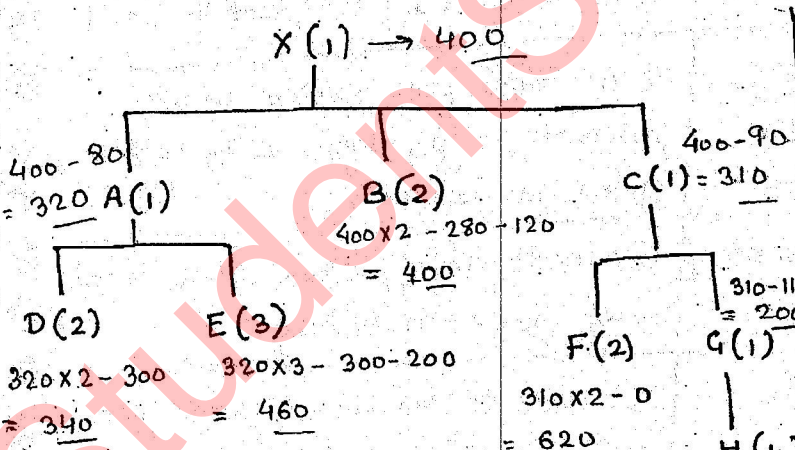
Net requirement = Gross Req. - [Inventory on hand + Scheduled Receipt]



week	P	R
1	1000	2000
2	1000	2000
3	1000	2000
4	1000	2000
5	1200	2400
6	1200	2400
		2166

Requirement of R per week.
 a) 1200 b) 2000
 c) 2200 d) 2400

Q - Find the net requirement for which we should place an order in order to produce 400 units of product X when inventory on hand and scheduled Receipt is as given below -

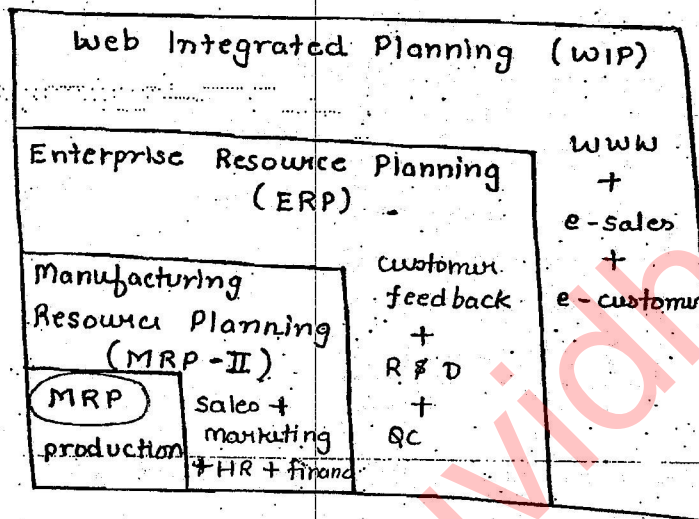


Inventory on hand	Scheduled Receipt
A - 80	B - 120
B - 280	D - 330
C - 90	E - 200
E - 300	H - 370
G - 110	
H - 330	

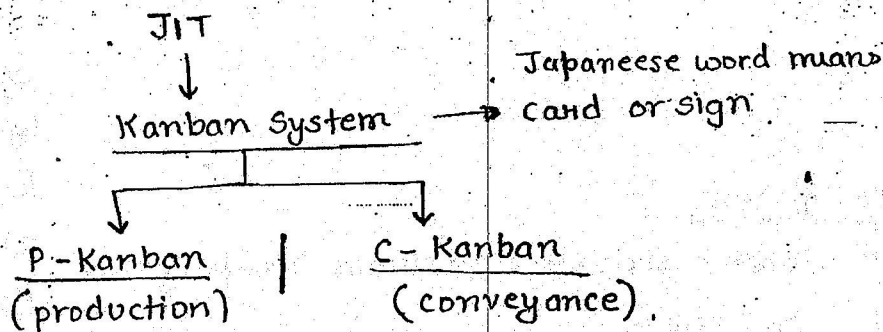
- B = 400
- D = 340
- E = 460
- F = 620
- H = 100

Advantages of MRP :-

- i) It help us to know when and how much to order
- ii) It help in inventory reduction.
- iii) It helps to avoid delay in production.
- iv) It gives timely information to marketing department about expected delivery time.



MRP	JIT (Just In Time)
It is from push system where product is produced in advance to meet the future requirement.	It is from pull system where product is produced only when there is demand.
Keep safety stock along with inventory.	Eliminate safety stock and keep very less inventory.
It can handle dynamic condition where demand suddenly changes.	Not able to handle dynamic condition as incapable of taking sudden and large variation.
No need to maintain good relation with the vendor.	Need to maintain good relation with vendor to get timely information.
It is preferred for batch or job type product.	It is preferred for mass product.



Reliability and failure Analysis :- (ES only)

Reliability is the ability of the product to perform its main function properly for a specified period of time under the given operating conditions. A product is reliable by that we mean that it will function in the manner as expected of it.

Reliability include 4 important factors -

- i) Probability
- ii) Time
- iii) Function or performance
- iv) Operating condition or environment.

Failure : The variation in the properties of a product from the desired condition is termed as failure. It represents unreliability. A product is considered to be fail when

- i) It become completely inoperable
- ii) when it is still operable but not able to perform
- iii) when its continuous use may be not safe / unsafe.

Cause of failure -

- i) defect in design
- ii) improper selection of manufacturing process and technique
- iii) Lack of knowledge and experience
- iv) Error during assembly
- v) Improper maintenance
- vi) Variation in the operating condition
- vii) human error

Types of failure :-

1) Catastrophic (chance) failure :-

A normal operating product suddenly becomes inoperative without any warning, eg - bulb.

2) Degradation (creeping) failure :-

It occurs gradually because of change in some parameter with time.

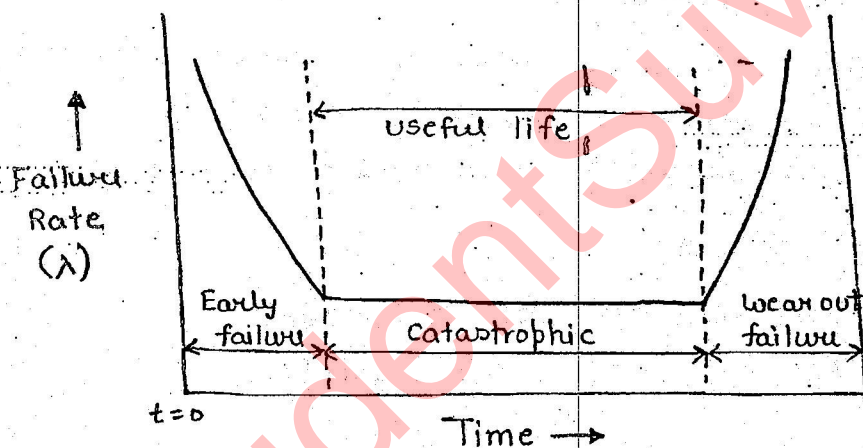
3) Independent (primary) failure :-

These are the failures which occur independently and does not depend upon the failure of others.

4) Dependent (secondary) failure :-

These products fail due to some primary failure.

Phase of Failure (Bath Tub Curve)



Early failure :- These failures occur at the beginning due to defective design, mfg or assembly work. Warranty is based on the concept of early failure.

Catastrophic :- These failures occur randomly or suddenly. These are caused due to sudden stress accumulation beyond designed limit.

wear out failure :- It is typical ageing problem and product will fail out due to tear and wear. Proper care and maintenance can delay the failure.

Terms related to Reliability -

Failure Rate (λ) :- The no. of failures per unit time is termed as failure rate and is normally expressed in terms of failure per 100 hrs or 1000 hrs.

$$\lambda = \frac{\text{No. of failure}}{\text{Time}}$$

eg : 4000 hrs \rightarrow 8 failure

$$\lambda = \frac{8}{4000} = \underline{\underline{2 \text{ failure} / 1000 \text{ hrs}}}$$

Mean time between failure :- It is the time gap b/w two successive failure.

$$\text{MTBF} = \frac{1}{\lambda}$$

Mean time to failure :- It is the average time a product is expected to function before getting fail. It is used for those product which can not be repaired.

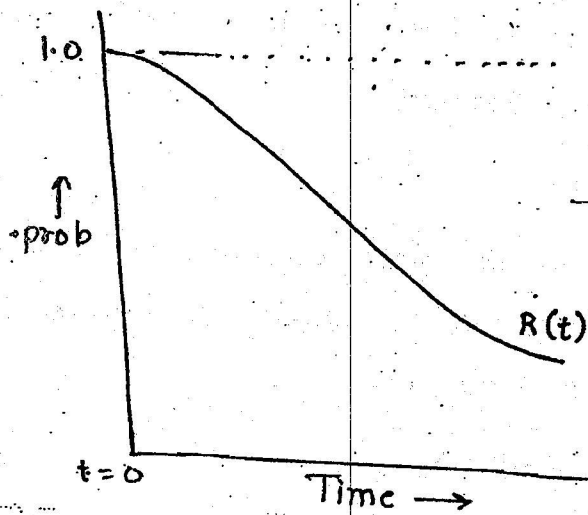
If $t_1, t_2, t_3, \dots, t_n$ are time to failure.

$$\text{MTTF} = \frac{\sum_{i=1}^n t_i}{n}$$

Reliability function ($R(t)$) :- It indicates the probability that the product will function over a period of time (t).

$$R(t) = \text{Prob} \{T \geq t\}$$

T is the time to failure



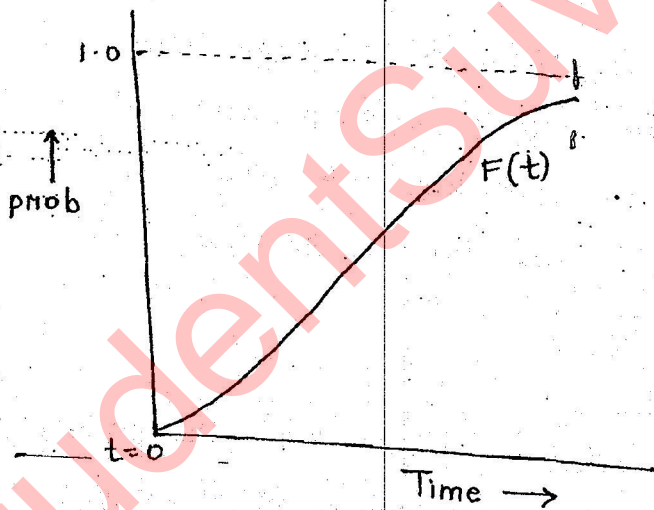
Failure function or cumulative distributive function :-

It is the probability that failure occurs before some period of time 't'

$$F(t) = 1 - R(t)$$

$$F(t) = \text{Prob} \{ T < t \}$$

$T \rightarrow$ time of failure.

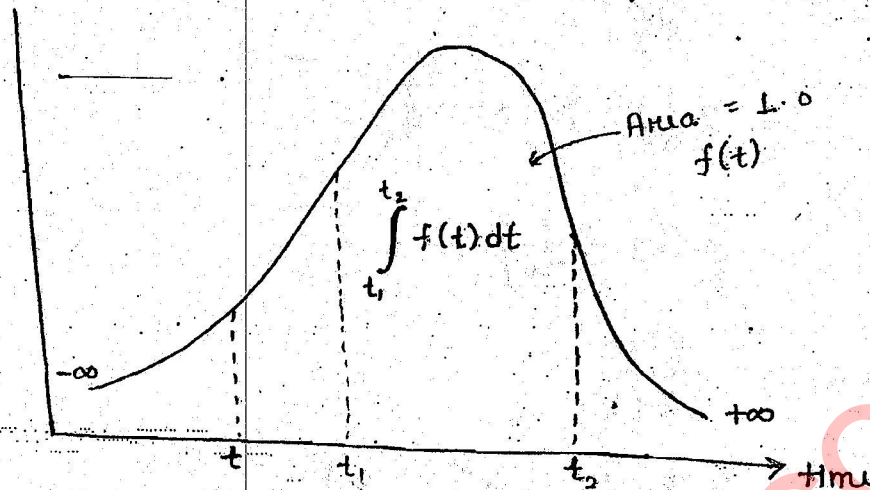


Probability density function :- This function describe the shape and the area of failure distribution.

$$f(t) = \frac{d F(t)}{dt} = - \frac{d R(t)}{dt}$$

$$R(t) = \int_t^{\infty} f(t) dt$$

$$F(t) = \int_{-\infty}^t f(t) dt$$



Important Formula

$$1) F(t) = 1 - R(t)$$

$$2) f(t) = \frac{dF(t)}{dt} = -\frac{dR(t)}{dt}$$

$$3) R(t) = \int_t^{\infty} f(t) dt$$

$$4) F(t) = \int_{-\infty}^t f(t) dt$$

$$5) \text{MTTF} = \int_0^{\infty} R(t) dt$$

$$6) \lambda(t) = \frac{f(t)}{R(t)}$$

Q - The reliability of a cutting assembly is as given below.

Determine -

i) Failure rate

ii) Does failure rate inc. or decrease with time

iii) MTTF.

$$R(t) = \begin{cases} \left(1 - \frac{t}{t_0}\right)^2 & 0 \leq t \leq t_0 \\ 0 & t \geq t_0 \end{cases}$$

$$1) f(t) = - \frac{dR(t)}{dt}$$

$$= - 2 \left(1 - \frac{t}{t_0}\right) \times - \frac{1}{t_0}$$

$$= \frac{2}{t_0} \left(1 - \frac{t}{t_0}\right)$$

$$\lambda(t) = \frac{f(t)}{R(t)}$$

$$= \frac{\frac{2}{t_0} \left(1 - \frac{t}{t_0}\right)}{\left(1 - \frac{t}{t_0}\right)^2}$$

$$= \frac{2}{t_0} \times \frac{t_0}{t_0 - t} \Rightarrow \frac{2}{t_0 - t}$$

$$2) \text{ At } t = 0, \lambda(t) = \frac{2}{t_0}$$

$$\text{At } t = t_0, \lambda(t) \Rightarrow \infty$$

failure rate is increasing with time.

$$3) \text{ MTTF} = \int_0^{\infty} R(t) dt$$

$$= \int_0^{\infty} \left(1 - \frac{t}{t_0}\right)^2 dt$$

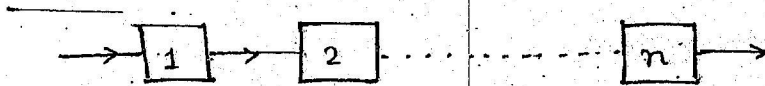
$$= \int_0^{\infty} \left(1 + \frac{t^2}{t_0^2} - \frac{2t}{t_0}\right) dt$$

$$= \left[t + \frac{t^3}{3t_0^2} - \frac{2t^2}{2t_0} \right]_0^{\infty}$$

$$= \frac{t_0}{3}$$

System Reliability

i) Component connected in series :-

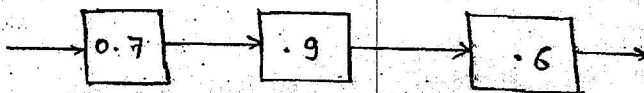


$$R_s \leq \min \{ R_i \}$$

$$R_s = R_1 \cdot R_2 \cdot R_3 \cdot \dots \cdot R_n$$

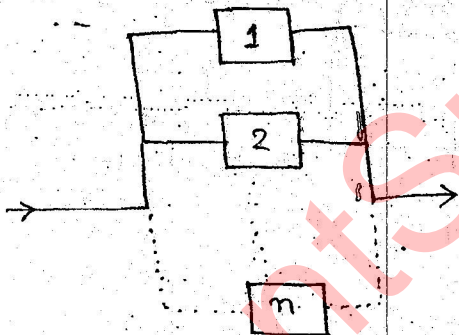
For the successful operation of the system all the component connected in series must be working.

for eg -



$$\begin{aligned} R_s &= 0.7 \times 0.9 \times 0.6 \\ &= \underline{\underline{0.378}} \end{aligned}$$

ii) Component connected in parallel :-

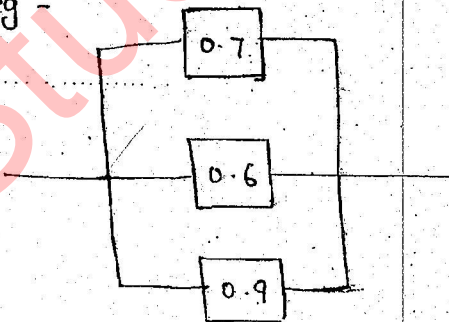


$$R_s \geq \max \{ R_i \}$$

$$R_s = 1 - [(1 - R_1) \cdot (1 - R_2) \cdot \dots \cdot (1 - R_n)]$$

For the successful operation of the system any one component in parallel must be working.

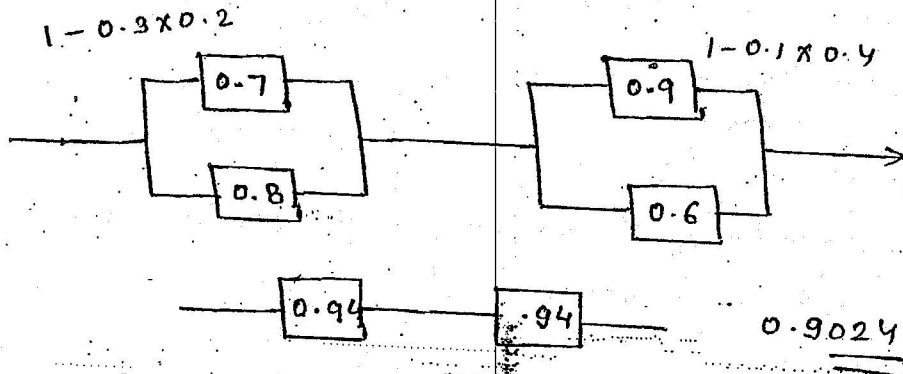
for eg -



$$\begin{aligned} R_s &= 1 - [0.3 \times 0.4 \times 0.1] \\ &= \underline{\underline{0.988}} \end{aligned}$$

iii) Combined Series parallel System :-

The reliability of the system is analysed by converting them into equivalent sub system.



Q - Find the reliability of the system as given below.

