

* CONSTRUCTION OF PREDICTIVE PARSING TABLE PROCEDURE - :

for each production $A \rightarrow \alpha$ apply the following steps to fill the entries of the predictive parsing table, $M[A, a]$ - :

- ①. Add $A \rightarrow \alpha$ to the $M[A, a] \forall a \in \text{FIRST}(\alpha)$
- ②. Add $A \rightarrow \alpha$ to $M[A, a] \forall b \in \text{FOLLOW}(A)$ if $\text{FIRST}(\alpha)$ contains ϵ .
- ③. make all other entries as error.

PREDICTIVE PARSING ALGORITHM - :

Let x be the symbol on Top of the Stack
 a be the symbol under input pointer
then the parser behaves as follows - :

- ①. If $x = a \neq \$$, then pops off x from the stack; and advance ip pointer to the next symbol.
- ②. If $x = a = \$$, parser announces successful completion of parsing.
- ③. If x is a Non Terminal, and the parsing program context contacts Predictive parsing Table Entry $M[x, a]$.

Suppose $M[x, a] = x \rightarrow uvw$ then parser replaces x by wvu with u on top.

Suppose $M[x, a] = \text{error}$, the parser calls error recovery unit.

Q. Construct predictive parsing Table for the following grammar. G_1 .

- (1) $S \rightarrow AB$
 $A \rightarrow aBb | \epsilon$
 $B \rightarrow b.$

X	first(x)	follow(x)
S	a, b.	\$
A	a, ϵ	b
B	b	\$, ϵ

Predictive Table - :

	a	b	\$
S	$S \rightarrow AB$	$S \rightarrow AB$	ERR
A	$A \rightarrow a$	$A \rightarrow \epsilon$	ERR
B	ERR	$B \rightarrow b.$	ERR

- (2) $S \rightarrow AB\epsilon$
 $A \rightarrow aBb | \epsilon$
 $B \rightarrow b | \epsilon.$

Predictive Table - :

	a	b	ϵ	ϵ \$
S	$S \rightarrow AB\epsilon$	$S \rightarrow AB\epsilon$	$S \rightarrow AB\epsilon$	ERR
A	$A \rightarrow aBb$	$A \rightarrow \epsilon$	$A \rightarrow \epsilon$	ERR
B	ERR	$B \rightarrow b$ $B \rightarrow \epsilon$	$B \rightarrow \epsilon$	ERR

Proves in this way.

X	FIRST(X)	FOLLOW(X)
S	{a, b, e}	{ \$ }
A	{a, ε}	{ b, e }
B	{b, ε}	{ b, e }

③

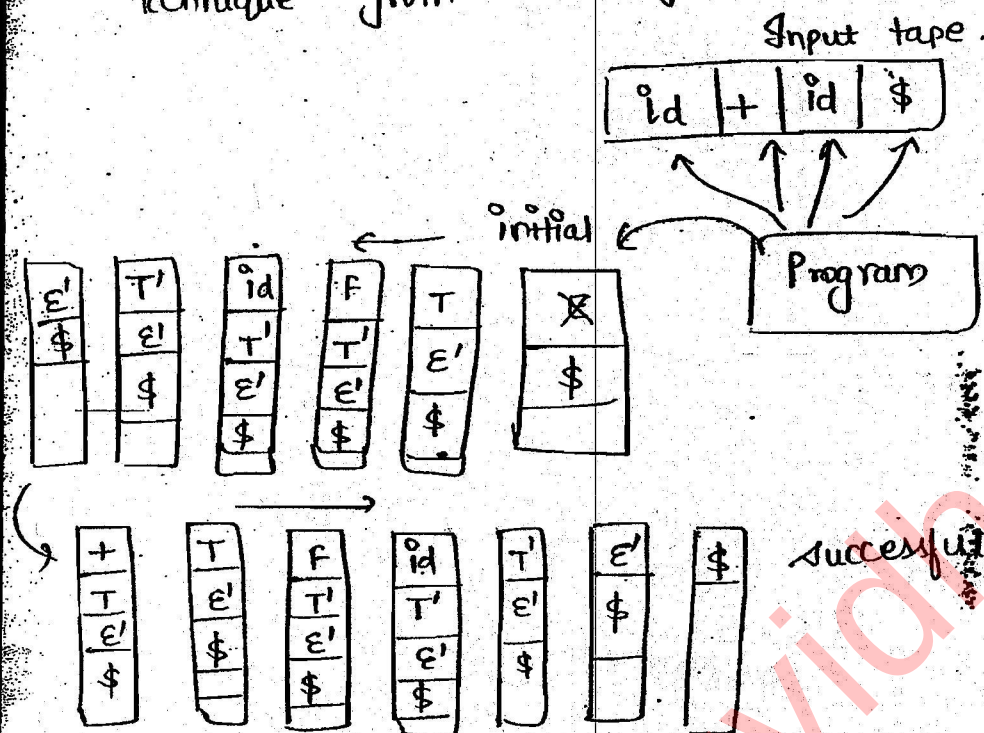
$$\begin{aligned}
 E &\rightarrow TE' \\
 E' &\rightarrow +TE' \mid \epsilon \\
 T &\rightarrow FT' \\
 T' &\rightarrow *FT' \mid \epsilon \\
 F &\rightarrow (E) \mid id
 \end{aligned}$$

X	FIRST(X)	FOLLOW(X)
E	(, id	\$,)
E'	+, ε	\$,)
T	(, id	+, \$,)
T'	*, ε	+, \$,)
F	(, id	*, +, \$,)

Predictive Table -

	+	*	(	)	id	\$
E	ERR	ERR	$E \rightarrow TE'$	ERR	$E \rightarrow TE'$	ERR
E'	$E' \rightarrow +TE'$	ERR	ERR	$E' \rightarrow \epsilon$	ERR	$E' \rightarrow \epsilon$
T	ERR	ERR	$T \rightarrow FT'$	ERR	$T \rightarrow FT'$	ERR
T'	$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$	ERR	$T' \rightarrow \epsilon$	ERR	$T' \rightarrow \epsilon$
F	ERR	ERR	$F \rightarrow (E)$	ERR	$F \rightarrow id$	ERR

Trace the string $id + id$ using predictive parsing technique from above grammar.



* LL(1) grammars.

A grammar G is said to be LL(1) if predictive parsing table do not contains multiple define entries for given G . (The LL(1) stands for -

- ① The first L represents in LL(1) represents left to right scan of the input string.
- ② The second L represents leftmost derivation.
- ③ 1 represents use one symbol as a lookahead at a time.

Q. Check whether the following grammar is LL(1) or not - 0.

① $S \rightarrow ABe$
 $A \rightarrow Aa|b$
 $B \rightarrow e$

Left Recursive grammar.

Kurki yha first (x) mai no E is the so no problem, it is a LL(1)

x	first(x)
S	b
A	b
B	e

	a	b	e	\$
S				
A		$A \rightarrow Aa$ $A \rightarrow b$		
B			$B \rightarrow e$	

Multiple entries so not LL(1)

Note - 0 Left Recursive grammars can have multiple entries in predictive parsing Table!
 So, Left Recursive grammar can not be LL(1)

② $S \rightarrow AB$
 $A \rightarrow ab|ad$
 $B \rightarrow b$

Left factored

so not LL(1)

	a	b	d	\$
S				
A	$A \rightarrow ab$ $A \rightarrow ad$			
B		$B \rightarrow b$		

Note - 0 Left factored grammar can not be LL(1) as they contain multiple entries in predictive parsing Table.

③

$$\begin{aligned} S &\rightarrow ictss' \\ S' &\rightarrow es \mid \epsilon \\ C &\rightarrow b. \end{aligned}$$

Ambiguous grammar.

	i	t	e	⊕ b	⊕
S	$S \rightarrow ictss'$				
S'			$S' \rightarrow es$ $S' \rightarrow \epsilon$		$S' \rightarrow \epsilon$
C				$C \rightarrow b$	

multiple entries.
not LL(1).

Ambiguous grammar can not be LL(1). Since they contain multiple entries.

CONCLUSION

Following grammar are not LL(1)

- ①. Left Recursive grammar
- ②. Left factored grammar
- ③. Ambiguous grammar.

SHORT CUT :-

To verify whether a given grammar G is LL(1) or not, we apply following conditions

- ①. for each non- ϵ productions,
 $A \rightarrow \alpha_1 \mid \alpha_2 \mid \alpha_3 \mid \dots \mid \alpha_n$, LL(1) grammar must hold
 $\text{FIRST}(\alpha_i) \cap \text{FIRST}(\alpha_j) = \phi$
 $\forall i \neq j.$

②. for all ϵ production of the form
 $A \rightarrow \epsilon$

The LL(1) grammar must hold,
 $\text{FIRST}(\alpha) \cap \text{Follow}(A) = \phi$

Don't worry about single productions (from a variable)

④. $S \rightarrow AB \mid BA$

$A \rightarrow aBb \mid \epsilon \Rightarrow \text{FT}(aBb) \cap \text{Follow}(A) \neq \phi$
 $\cap \{ \$, a, b \}$

$B \rightarrow Aa \mid b \Rightarrow \text{FT}(Aa) \cap \text{FT}(b)$
 $a \cap b = \phi$

do directly,

Do not LL(1).

~~$\text{Follow}(A) = \text{FT}(B)$~~

⑤. $E \rightarrow E+T \mid T$

$T \rightarrow T * F \mid F$

$F \rightarrow id \mid (e)$

Left recursive, do not LL(1).

Great perspective k acc. hume just given gram ko dekh kar blana hai. remove vgrh krik nai dekha.

agar hum issi grammar ko mai se left recursion remove kar dege to ye LL(1) ho shi hai (piche kia tha).

But it is not necessary that, if we remove left recursion and left factoring from a grammar, then it becomes LL(1), because then decision depends on ambiguous or not.

→ If ambiguous → not LL

→ If not ambiguous → LL.

Q. $A \rightarrow AA \mid (A) \mid \epsilon$ is not suitable for predictive parsing because the grammar is

- ☒ (a) ambiguous
- (b) Left Recursive
- (c) Right Recursive
- (d) An operator grammar.



as it is left Recursive as well as Right Recursive, so it is definitely ambiguous. So we always give priority to ambiguous.

Q. Which of the following is sufficient to convert an arbitrary CFG to an LL(1) grammar.

- (a) Removing left Recursion alone
- (b) factoring the grammar alone
- (c) Removing the left Recursion and factoring the grammar both.
- ☒ (d) None of the above.

↳ as it can be ambiguous still.

Q. Consider the following grammar -

$P \rightarrow x \mid R S$
 $Q \rightarrow y \mid z$
 $R \rightarrow w \mid \epsilon$
 $S \rightarrow y$

What is the follow of Q.

- ☒ (a) $R \rightarrow$ Never possible (NT).
- (b) w
- ☒ (c) w, y
- (d) w, \$

Q. Consider the following grammar shown below-:

$$S \rightarrow \text{~~ies~~ } iEtSS' \mid a$$

$$S' \rightarrow \underline{eS} \mid \underline{\epsilon}$$

$$E \rightarrow b.$$

In the predictive parsing table M of this grammar the entries $M[S', e]$ and $M[S', \$]$ respectively are — ?

- (a). $\{S' \rightarrow eS\}, \{S' \rightarrow \epsilon\}$
- (b). $\{S' \rightarrow eS\}, \{\}$
- (c). $\{S' \rightarrow \epsilon\}, \{S' \rightarrow \epsilon\}$
- (d). $\{S' \rightarrow eS, S' \rightarrow \epsilon\}, \{S' \rightarrow \epsilon\}$

By applying shortcut method, check directly.

Q. Consider the following grammar

$$S \rightarrow FR$$

$$R \rightarrow *S \mid \underline{\epsilon}$$

$$F \rightarrow id$$

In the predictive parsing table M of this grammar, the entries $M[S, id]$ and $M[R, \$]$ respectively

_____ ?

$$M[S, id] = S \rightarrow FR$$

$$M[R, \$] = R \rightarrow \epsilon$$

Q. Consider the following grammar shown below-:

$$S \rightarrow CC$$

$$C \rightarrow aC \mid d.$$

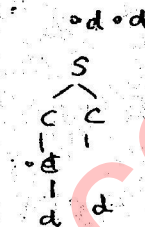
This grammar is — .

- (a) LL(1)
 (b) SLR(1) but not LL(1)
 (c) LALR(1) but not SLR(1)
 (d) LR(1) but not LALR(1)

This ~~valid~~ ^G is valid
 for all parse
 (It is unambiguous)

Q. Consider the following grammar -

$$\begin{aligned}
 E &\rightarrow E - T \mid T \\
 T &\rightarrow T + F \mid F \\
 F &\rightarrow (E) \mid id
 \end{aligned}$$



which of the following grammar is not left
 Recursive but is equal to G.

Sol. $\left\{ \begin{array}{l} E \rightarrow TE' \\ E' \rightarrow -TE' \mid \epsilon \\ T \rightarrow FT' \\ T' \rightarrow +FT' \mid \epsilon \\ F \rightarrow (E) \mid id \end{array} \right. \Rightarrow \left\{ \begin{array}{l} E \rightarrow TX \\ X \rightarrow -TX \mid \epsilon \\ T \rightarrow FY \\ Y \rightarrow +FY \mid \epsilon \\ F \rightarrow (E) \mid id \end{array} \right.$

Q. Consider the following grammar.

$$S \rightarrow aAbB \mid bAaB \mid \epsilon$$

$$A \rightarrow S$$

$$B \rightarrow S$$

① first and follow sets for the non terminals

X	A and B	first(X)	follow(X)
A		a, b, ϵ	a, b
B		a, b, ϵ	a, b, \$

Q. $S \rightarrow asa \mid bs \mid c$
 LL(1) or not?

$\Rightarrow$ LL(1)

Q. $S \rightarrow i c t s s_1 \mid a$
 $S' \rightarrow e s_1 \mid \epsilon$
 $c \rightarrow b$

The grammar is not LL1 because
it is ambiguous.

Q. 2016. Set 2. A student wrote 2 context free grammars G_1 and G_2 for generating a single C-like array declaration. The dimensions of array is atleast 1, for eg. $\text{int } a[10][3]$. The grammars use Δ as the start symbol and uses the 6 terminal symbols $\text{int } \text{id} [\text{num}] [\text{num}]$
 $*, \text{;}, \text{id}, (,), \text{no.}$

G_1
 $\Delta \rightarrow \text{int } L;$
 $L \rightarrow \text{id} [E$
 $E \rightarrow \text{num}]$
 $E \rightarrow \text{num}] [E$

G_2
 $\Delta \rightarrow \text{int } L;$
 $L \rightarrow \text{id } E$
 $E \rightarrow E[\text{num}]$
 $E \rightarrow [\text{num}]$

Which of the grammar correctly contains the declaration maintained above

(a) only G_1

(b) only G_2

(c) G_1 & G_2

(d) Neither G_1 nor G_2

Q. Which one of the following is Top down parser?

- ~~(a)~~ Recursive Descent parser
- (b) Operator precedence parser
- (c) LR(K)
- (d) LALR(K)

BOTTOM - UP PARSER

In bottom up parsing we attempt to construct a parse tree starting from leaf nodes and we work towards root node.

The primary objective of bottom up parsing is reducing the given string to start symbol.

In each step of the parsing, we identify the substring in a w that matches with right side string of some production (called Handle). Whenever we encounter a handle, we replace it by left side non-terminal of the production, this process is called reduction.

A bottom up parser is also called as shift reduce parser (SRP) in which the parser perform 4

actions namely shift, reduce, accept & error.

A shift reduce parser can be viewed as Right most derivation in reverse order.