

74457

M. Sc. (Mathematics) 2nd Semester Examination – May, 2016 OPERATIONS RESEARCH TECHNIQUES (NEW) w.e.f.

2014-15 Paper : MM-425-B

Time: Three Hours]

[Maximum Marks: 80

Before answering the questions, candidates should ensure that they have been supplied the correct and complete question paper. No complaint in this regard, will be entertained after examination.

Note: Attempt five questions in all, selecting one question from each of the four units I, II, III and IV. Unit-V contains one question with eight parts and is compulsory.

UNIT - I

(a) Discuss methodology and scope of operations research.

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- What are linear programming problems? Give mathematical formulation of general linear programming problem.
- Solve the following linear programming problem using Big-M method: 12

Maximize $Z = 3x_1 - x_2$

subject to constraints

$$2x_1 + x_2 \le 2$$

$$x_1 + 3x_2 \ge 3$$

$$x_2 \le 4$$

$$x_1, x_2 \ge 0$$

(b) Write a short note on 'duality' in linear programming.

UNIT - II

3. (a) What 'balanced' 'unbalanced' and transporation problem? Give one example of each. Explain how an unbalanced transporation is solved.

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(b) Solve the following transporation problem:

| 200 300 550 | turas en la companya de la companya | | · | | |
|-------------|--|--------|---|----|----|
| | | Supply | | | |
| | | 1 | 2 | 3 | |
| From | 1 | 2 | 7 | 4 | 5 |
| | 2 | 3 | 3 | 1 | 8 |
| | 3 | 5 | 4 | 7 | 7 |
| | 4 | 1 | 6 | 2 | 14 |
| Demand | | 7 | 9 | 18 | 34 |

10 (a) Solve the following assignment problem: Man

| | | I | <u> </u> | Ш | IV | V |
|------|---|---|----------|-----|-----|-----|
| | A | 1 | 3 | . 2 | 3 | 6 |
| | В | 2 | 4 | 3 | 1 | 5 |
| Task | C | 5 | 6 | 3 | 4 | · 6 |
| 24 | D | 3 | 1 | 4 | . 2 | 2 |
| | E | 1 | 5 | 6 | 5 | 4 |

(b) What is the travelling salesman problem? Which situations can be treated as the travelling

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salesman problem? How does its solution differ from the solution of the assignment problem?

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UNIT - III

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- **5.** (a) With respect to queue system, explain the following:
 - (i) Input process
 - (ii) Queue discipline
 - (iii) Traffic intensity
 - (iv) Steady state.
 - (b) Discuss M/M/C queuing model. Also give its important characteristics.
- 6. (a) A company uses Rs. 10,000 worth of an item during the year. The ordering costs are Rs. 25 per order and carrying charges are 12.5% of the average inventory value. Find the economic order quantity, number of orders per year, time period per order and the total cost.

(b) Explain the economic lot size model when shortages are allowed (instantaneous supply case).

UNIT - IV

- 7. (a) Explain the following terms and give one example of each:
 - (i) Two-person zero-sum game
 - (ii) Mixed strategy games,
 - (iii) Saddle point, and
 - (iv) Fair game.
 - (b) Solve the game whose pay-off matrix is given by:

R

| | | I | II | <u>III</u> | IV |
|---|-----|---|----|------------|----|
| | I | 3 | 2 | 4 | 0 |
| A | II | 2 | 4 | 2 | .4 |
| | III | 4 | 2 | 4 | 0 |
| | IV | 0 | 4 | 0 | 8 |

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- 8. (a) Discuss the concept of dominance in game theory.

 Give suitable example.
 - (b) Find an optimal sequence for the following sequencing problem involving four jobs and five machines when passing is not allowed, if each processing time (in hours) is given as under: 8

| Job | | Machine | | | | | |
|----------------|-------|----------------|----------------|----------------|----------------|--|--|
| | M_1 | M ₂ | M ₃ | M ₄ | M ₅ | | |
| Jı | 7 | 5 | 2 | 3 | 9 | | |
| J_2 | 6 | 6 | 4 | 5 | 10 | | |
| J ₃ | 5 | 4 | 5 | 6 | 8 | | |
| J4 | 8 | 3 | 3 | 2 | 6 | | |

Also find minimum elapsed time.

UNIT-V

- 9. (a) What do you mean by operations research? Explain,
 - (b) Differentiate between 'slack' and 'surplus' variables. Give suitable examples.
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- (c) Give mathematical formulation of general transporation problem.
- (d) What is a transhipment problem?
- (e) What are general birth-death equations?
- (f) Give any two objectives of the inventory control.
- (g) State maximin and minimax principle in game theory.
- (h) Mention four principal assumptions made while dealing with sequencing problems. 2×8

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