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(MS-3)

## GUJARAT TECHNOLOGICAL UNIVERSITY

B.E. all Sem-I Examination December 08/January 09

## MECHANICS OF SOLIDS (110010)

DATE: 19-12-2008, Friday TIME: 12.00 to 2.30 p.m. MAX. MARKS: 70

## Instructions:

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.
4. Use of graph paper is permitted
Q.1(a) Fill in the blanks with most appropriate answer.
(i) Lateral strains are __ longitudinal strains. Falways less than, sometimes less than, never less than)
(ii) Two forces under equilibrium must be C non rectilinear, rectilinear, parallel)
(iii) True relation between dynamic coefficient of friction ( $\mu_{\mathrm{d}}$ ) and static coefficient of friction ( $\mu_{s}$ ) is $\qquad$ $\left(\mu_{\mathrm{d}}>\mu_{\mathrm{s}}, \mu_{\mathrm{d}}=\mu_{\mathrm{s}}, \mu_{\mathrm{d}}<\mu_{\mathrm{s}}\right)$
(iv) $\qquad$ is a scalar quantity.(momentum, force, work)
(v) $100 \mathrm{~mm}=$ $\qquad$ $\mu \mathrm{m}\left(10^{5}, 10^{6}, 10^{-7}\right)$
(b) Do as Directed
(i) Sketch principal planes for the elements subjected to following stresses on two mutually perpendicular planes. (1) Only direct stresses (2) Only shear stresses.
(ii) Differentiate between: (1) Moment of couple $\mathrm{v} / \mathrm{s}$ moment of force (2) angle of repose varangle of friction.
(iii) Draw typiftar stress - straín plot for a tension test results of mild steel bar. Show \&anent points on it.
Q.2(a) Derive ${ }^{\text {Ko }}$,
(i) Moment of Inertia of rectangular Lamina @ its centroidal axis using first principle.
(ii) Relation between uniformly distributed load, shear force and bending moment with usual notations.
(b) In a differential wheel and axle, the diameter of an effort wheel is 500 mm and the diameter of axles is 200 mm and 100 mm . This machine needs an effort of 550 N to lift 2 kN load and an effort of 800 N to lift 4 kN load. Find .(i) Law of machine (ii) Max efficiency (iii) Effort lost in friction and efficiency at 3 kN load.

## OR

(b) A 4 m long ladder has to carry a person of 75 kg weight at 3.5 m distance from floor, along the length of ladder. The self weight of ladder is of 150 N . Find the maximum distance of lower end of ladder from vertical wall so that it does not slide. The coefficient of friction between floor and ladder is 0.3 and that between vertical wall and ladder is 0.2 .
Q.3(a) An assembly of steel bars as shown in the fig. 1 is in equilibrium. Find force $P$
and the net elongation of the assembly. Take $\mathrm{E}_{\mathrm{s}}=2 \times 10^{5} \mathrm{MPa}$.
(b) For the beam shown in fig.2, calculate shear force and bending moments at

## OR

Q.3(a) Sketch qualitative shear stress distribution diagrams across the (i) Hollow square (ii) H sections and (iii) T section of the beams.
(b) A mild steel simply supported beam of 3 m span has cross section 20 mm (width) x 50 mm (depth). Find the maximum uniformly distributed load that beam can carry in addition to its self weight, if maximum bending and shear stresses are limited to $150 \mathrm{~N} / \mathrm{mm}^{2}$ and $100 \mathrm{~N} / \mathrm{mm}^{2}$. Self weight of beam is $75 \mathrm{~N} / \mathrm{m}$.
Q.4(a) Find resultant of a force system shown in fig. 3

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(b) Find support reactions for the beam shown in the fig. 4 04
(c) Find center of gravity of a lamina shown in the fig. 5 .

OR
Q.4(a) Find the magnitude of the force P , required to keep the 100 kg mass in the position by strings as shown in the fig. 6 .
(b) Locate zero force members in truss shown in the fig.7. Also find axial forces in remaining members.
(c) Find Moment of Inertia of a lamina shown in the fig. 8 about horizontal centroidal axis.
Q.5(a) Prove that maximum shear stress in circular section of a beam is $4 / 3$ times of04 average shear stress.
(b) Determine change in volume of a steel bar of 100 mm dia.and 500 mm length, when it is subjected to axial pull of 50 kN . Take $\mathrm{E}_{\mathrm{s}}=200 \mathrm{GPa}$ and Poisson ratio 0.25
(c) An assembly made up from Aluminium and Steel bars as shown in the fig.9, is initially stress free at temperature $32^{\circ} \mathrm{C}$. The ass embly is heated to bring its temperature to $82^{\circ} \mathrm{C}$. Find the stresses developed in each bar. The coefficient of thermal expansions, is $1.25 \times 10^{-5}{ }^{\circ} \mathrm{C}$ \& $2.25 \times 10^{-5} / \mathrm{C}$ for steel and aluminium respectivelg. Take $\mathrm{E}_{\mathrm{s}}=200 \mathrm{GPa} \& \mathrm{E}_{\mathrm{al}}=75 \mathrm{GPa}$.

## OR

Q.5(a) A rectangular 480 den beam of size $200 \times 300 \mathrm{~mm}$ is strengthen by steel plates of 10 , rin thickness covering entire width of wooden section at top and bottom . Fi a the moment carrying capacity of the composite section if allowablestresses in wood and steel are 20 MPa and 100 MPa respectively. Take modular ratio as 10.
(b) For an element shown in fig. 10 find: (i) principal stresses and location of correspondíng principal planes. (ii) Maximum shear stress and location of planes containing it.


Fig. 2 Q. 3 (b)


Fig. 3 Q-4 (a)


Fig. 4 Q. 4 (b)


Fig. 5 Q-4 (c)


Fig. 8 Q-4 (c)OR


Fig. 9 Q. 5 (c)


Fig. 10 Q-5(b) OR

