

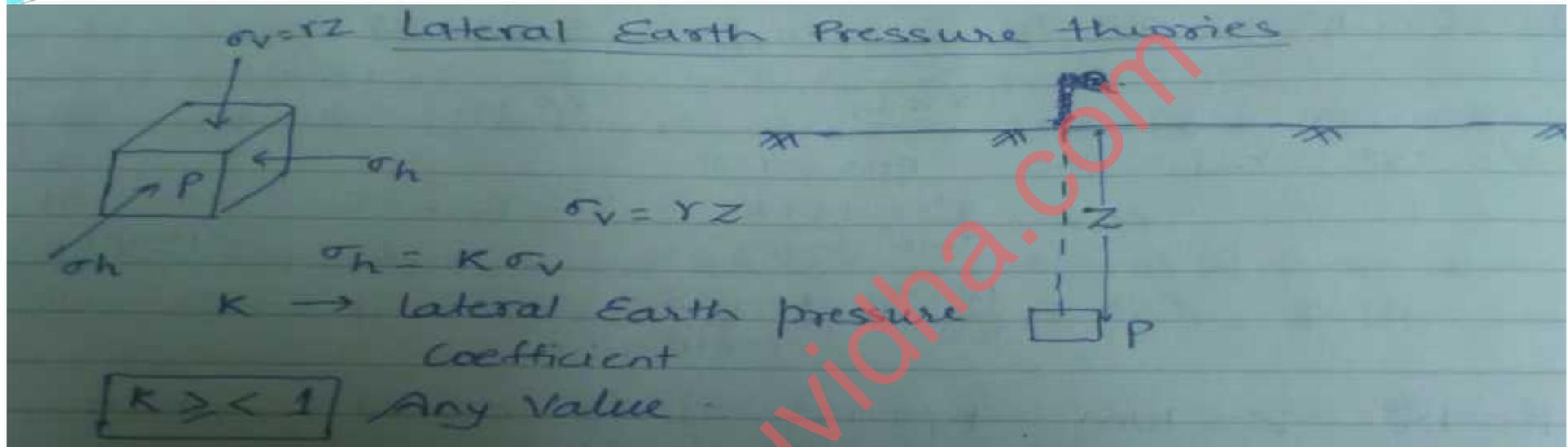
# *Unit-X: LATERAL EARTH PRESSURE*

By Tanuj Gupta

# Unit-X: *Earth Pressure*

- Introduction, earth pressure at rest, Rankine's active & passive states of plastic equilibrium, Rankine's earth pressure theory, Coulomb's earth pressure theory, Culmann's graphical construction, Rebhann's construction.

# LATERAL EARTH PRESSURE



- There are three states of Lateral Earth Pressure
  - Active State
    - Wall moves away from fill ( $K = K_a$ )
  - At rest state
    - Wall is stationary ( $K = K_0$ )
  - Passive State
    - Wall pushed against the soil/towards soil ( $K = K_p$ )

# LATERAL EARTH PRESSURE

- Earth pressure at rest
  - If the wall is stationary then lateral earth pressure at any depth  $z$  is

$$\dagger_h = p_o = k_o \gamma z$$

- If lateral strain is zero  $\epsilon_h = 0$

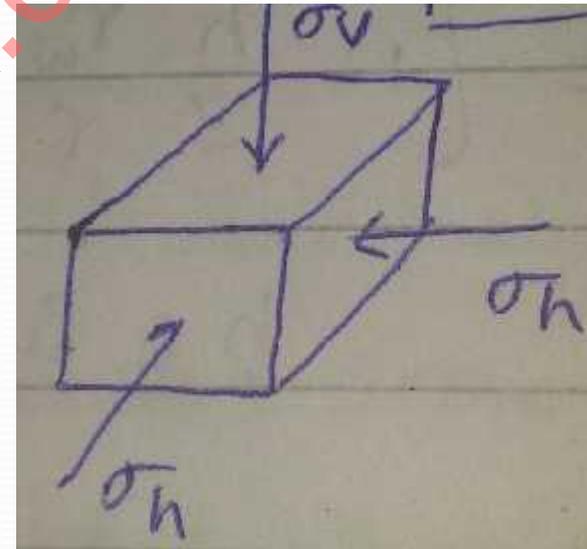
$$-\frac{\dagger_h}{E} + \frac{\dagger_v}{E} + \frac{\dagger_h}{E} = 0$$

$$\dagger_h = \frac{\dagger_v}{(-1)}$$

$$\dagger_h = k_o \dagger_v$$

- If friction angle of soil  $\phi$  is then  $K_o$  is given by

$$k_o = 1 - \sin \phi$$

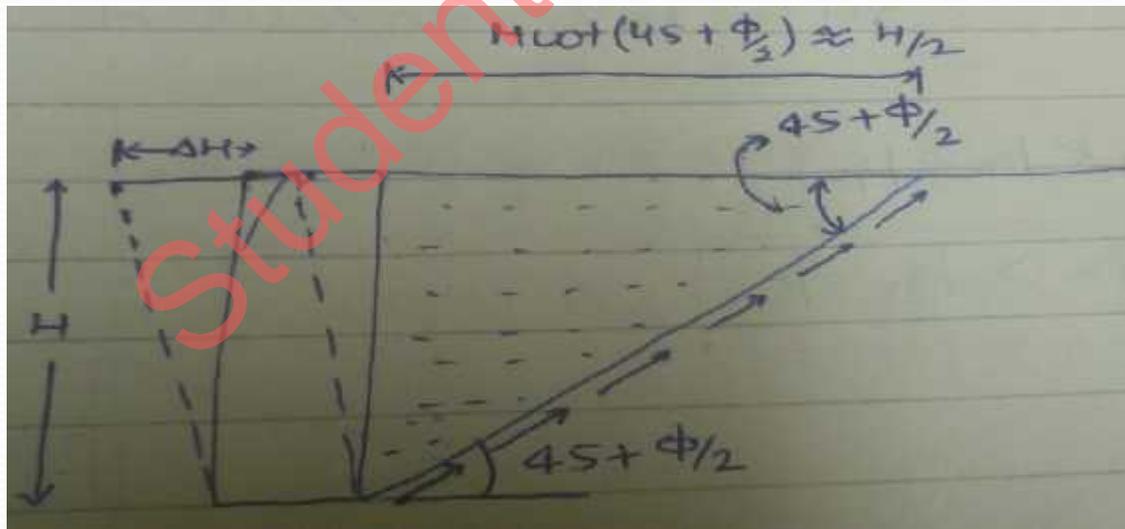


# LATERAL EARTH PRESSURE

- Active earth Pressure
  - In active state, earth pressure is less than earth pressure at rest because when wall moves away from backfill then mobilization of internal resistance in the soil occur
  - At any depth  $z$  from ground level active earth pressure

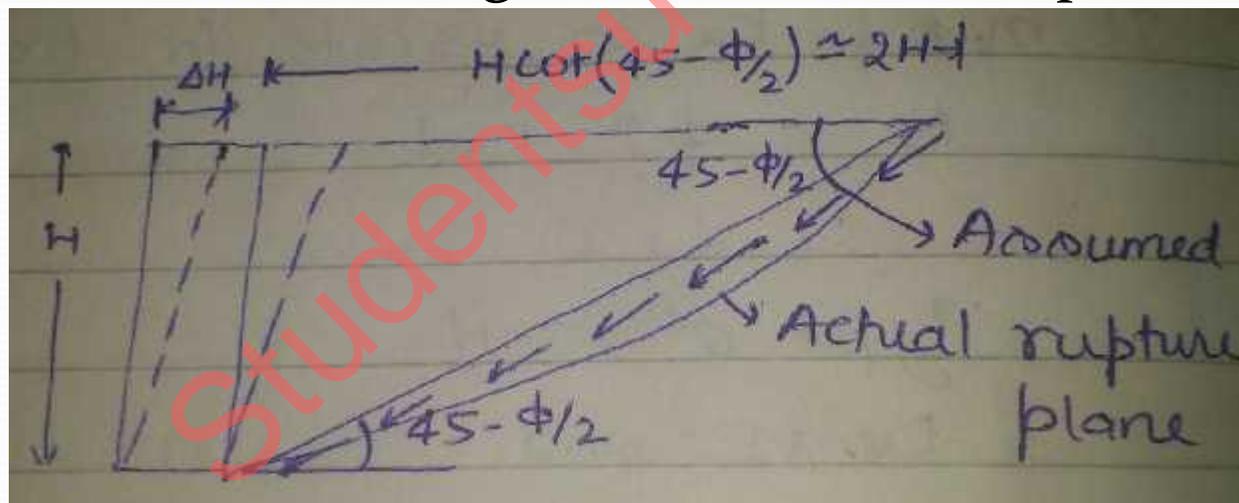
$$p_a = k_a \gamma z$$

- Where  $K_a$  is active earth pressure coefficient



# LATERAL EARTH PRESSURE

- Passive earth pressure
  - In passive state, the wall is pushed against the backfill of soil
  - The passive earth pressure is greater than the earth pressure at rest because when wall is pushed against the backfill the shearing resistance is built up in the soil



# LATERAL EARTH PRESSURE THEORIES

- Though Coulomb's theory was given first and Rankine's theory was an improvement over Coulomb's theory but Rankine's theory is more versatile due to its simplicity
- Coulomb considered inclined and rough wall whereas Rankine considered vertical and smooth wall
- Coulomb considered wedge failure whereas Rankine considered element failure
- In Coulomb's theory, the position and direction of resultant thrust is known
- Both theories considered the soil mass to be dry, cohesionless, homogeneous, isotropic and elastic
- For RCC and masonry walls Coulomb's theory is more practical whereas for metallic surface Rankine theory is better
- In case of passive earth pressure, Coulomb's theory is less accurate because in passive state, failure surface is curved & Coulomb's is approximated to the plane surface

# RANKINE THEORY

- Assumptions
  - Soil mass is semi-infinite, homogeneous, dry and cohesionless
  - The ground surface of backfill soil is plane which may be horizontal or inclined
  - The face of the wall in contact with the backfill is vertical and smooth
  - The wall yields about the base sufficiently to mobilise full active and passive state
  - The stresses in the soil are considered when failure occurs at rupture surface and at the time of failure soil reaches in plastic state
  - Rankine considered element failure. He made analysis by considering equilibrium of an element

# RANKINE THEORY

$$p_a = k_a \lambda H$$

$$p_p = k_p \lambda H$$

$$K_a = \frac{(1 - \sin \phi)}{(1 + \sin \phi)} = \tan^2 \left( 45 - \frac{\phi}{2} \right)$$

$$K_p = \frac{(1 + \sin \phi)}{(1 - \sin \phi)} = \tan^2 \left( 45 + \frac{\phi}{2} \right)$$

$$K_a < K_o < K_p \quad K_a = \frac{1}{K_p}$$

