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B.Tech. (CSE/IT) (Sem.-4th) MATHEMATICS-III Subject Code : CS-204 Paper ID : [A0495]

Time : 3 Hrs.

Max. Marks: 60

## **INSTRUCTION TO CANDIDATES :**

- 1. SECTION-A is COMPULSORY.
- 2. Attempt any FOUR questions from SECTION-B.
- 3. Attempt any TWO questions from SECTION-C.

## SECTION-A

 $(10 \times 2 = 20 \text{ Marks})$ 

- 1. (a) State Cauchy's mean value theorem.
  - (b) Evaluate  $\iint (x + y) dy dx$  over the region bounded by  $x = 0, y = 0, x^2 + y^2 = 9.$
  - (c) Evaluate  $\int_0^{1+i} (x^2 iy) dz$  along the path,  $y = x^2$ .
  - (d) Expand sin z by Taylor's series about the point  $\frac{\pi}{4}$ .
  - (e) For the conformal transformation  $w = z^2$ , find the angle of rotation at z = 1 + i.
  - (f) A rod of length l with insulated sides is initially at a uniform temperature  $u_0$ . Its ends are suddenly cooled to 0°C and are kept at that temperature. If it is required to find the temperature function u(x,t) then write down the initial and the boundary conditions.
  - (g) State the fundamental theorem of integral calculus.
  - (h) Use Picard's method to solve the equation,  $\frac{dy}{dx} = x + y^2$ , given that y(0) = 0.
  - (i) Write the formulae for the Runge-Kutta method of order 4.
  - (j) Determine the residue at the pole of order 2 for the function  $f(z) = \frac{z^2}{(z-3)(z-2)^2}$

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## **SECTION-B**

(4 × 5 = 20 Marks)

- 2. Obtain the value of the triple integral  $\iiint (x + y + z)dx dy dz$  over the tetrahedron bounded by the co-ordinate planes and the plane, x + y + z = 1.
- 3. State and prove the Cauchy's integral formula.
- 4. Expand,  $f(z) = \frac{1}{(z+1)(z+3)}$  valid for (*i*) 1 < |z| < 3, (*ii*) 0 < |z+1| < 2.

5. Use Taylor series method to solve  $\frac{dy}{dx} = x^2 - y$  at x = 0.1, given that y(0) = 1.

6. Solve the partial differential equation,  $\frac{\partial u}{\partial t} = C^2 \frac{\partial^2 u}{\partial x^2}$ , the boundary conditions are u(0,t) = 0, u(l,t) = 0 (t >0) and initial condition is u(x,0) = x, *l* being the length of the bar.

**SECTION-C**  $(2 \times 10 = 20 \text{ Marks})$ 

7. A string is stretched and fastened to two points l apart. Motion is started by displacing the string in the form  $y = a \sin \frac{\pi x}{l}$  from which it is released at time t = 0. Show that the displacement of any point at a distance x from one end at time t is given by,  $y(x,t) = a \sin \frac{\pi x}{l} \cos \frac{\pi ct}{l}$ 

8. Evaluate  $\int_{-\infty}^{\infty} \frac{x^2}{(x^2+a^2)(x^2+b^2)} dx$ , (a > 0, b> 0), using the concept of contour integration.

9. Find the values of u(x,t) satisfying the parabolic equation,  $\frac{\partial u}{\partial t} = 4 \frac{\partial^2 u}{\partial x^2}$ and the boundary conditions u(0,t) = 0 = u(8,t) and  $u(x,0) = 4x - \frac{x^2}{2}$ at the points x = i: i = 0,1,2,...,7 and  $t = \frac{1}{8}$  j : j = 0,1,2,...,5.

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