$\qquad$
$\qquad$

## GUJARAT TECHNOLOGICAL UNIVERSITY <br> BE - SEMESTER-VII • EXAMINATION - SUMMER • 2014

## Subject Code: 171901

Date: 22-05-2014
Subject Name: Operation Research
Time: 02:30 pm - 05:00 pm
Total Marks: 70

## Instructions:

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.
Q. 1 (a) State the phases of Operation Research. Discuss in brief the areas of application of Operation Research
(b) Solve the following LPP by simple method :

Maximize $Z=3 x_{1}+2 x_{2}$ subject to $2 x_{1}+x_{2} \leq 5, x_{1}+x_{2} \leq 3$ and $x_{1}$ and $x_{2} \geq 0$
Q. 2 (a) Company wants to find out the minimum time require to complete four tasks by available four workers with him so that he can take another from the order party. Following table gives the time in hours for each workers for each job

|  | A | B | C | D |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 24 | 10 | 21 | 11 |
| 2 | 14 | 22 | 10 | 15 |
| 3 | 15 | 17 | 20 | 19 |
| 4 | 11 | 19 | 14 | 13 |

(b) Explain Monte Carlo simulation procedure. Also discuss its applications with suitable example

## OR

(b) A school wants to pive up students from five different areas. Cost in rupees of going from one ate to another is shown in table. Find the optimal route to the bus drive such at no repetition of the area comes before picking up students from all areas?

|  | II | III | IV | V |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| IV | 0 | 30 | 60 | 80 | 20 |
| II | 70 | 0 | 40 | 90 | 30 |
| III | 90 | 80 | 0 | 50 | 80 |
| IV | 130 | 50 | 70 | 0 | 60 |
| V | 20 | 40 | 30 | 90 | 0 |

Q. 3 (a) Reduce following matrix by rule of dominance

| Player |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Bl |  |  |  |  | B2 | B3 | B4 |
|  |  | B1 | 6 | 4 | 8 |  |  |  |  |
| 0 |  |  |  |  |  |  |  |  |  |
|  | A2 | 6 | 8 | 4 | 8 |  |  |  |  |
|  | A3 | 8 | 4 | 8 | 0 |  |  |  |  |
|  | A4 | 0 | 8 | 0 | 16 |  |  |  |  |

(b) Two companies are thinking on selecting the advertising media. There are three medias available along with the pay of as shown in the pay of matrix

|  |  | TV | Radio | Internet |
| :---: | :---: | :---: | :---: | :---: |
| Player A | TV | 150 | 200 | -400 |
|  | Radio | 0 | 75 | -100 |
|  | Internet | 450 | 100 | 250 |

Value is in gain sales in (1000 rupees) suggest optimal strategy for the marketing and find out the value of the game
Q. 3 (a) A person is planning to purchase a car. A new car is costing rupees 3 lacs. The resale value of the car at the end of the year is $85 \%$ of the previous year. Maintenance and repair cost during the first year are rupees 10000 and they increase by $15 \%$ every year. The minimum resale value of the car can be rupees 75000 . (a) When should the car be replaced to minimize average annual cost? (b) If interest rate of $12 \%$ is assumed, calculate the average cost at the end of 10 years
(b) A copy maker has one copy making machine and he operates as the order comes. The order arrival is poison distribution having interval time of 0.5 min . The average time to serve a copy is distributed with mean of 0.3 min . Determine the following: (1) Utilization factor of the machine (2) Idle time for machine in a day having working hours of 10 hours (3) No of persons waiting in the system (4) No of persons waiting in the queue (5) Average waiting time in the queue
Q. 4 (a) From the following given data find out shortage cost for the item. $\mathrm{C}_{1}=$ Rs.900/and critical probability $=0.70$

| Units Stocked | 50 | 58 | 65 | 70 | 75 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Probability | 0.2 | 0.25 | 0.14 | 0.34 | 0.07 |

(b) Consider the following given data and based on that find out critical path for the given project.

| Activity | $1-2$ | $1-3$ | $2-4$ | $3-4$ | $3-5$ | $3-6$ | $4-6$ | $5-6$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Time in <br> days | 6 | 9 | 3 | 4 | 8 | 12 | 7 | 1 |

OR
Q. 4 (a) A utensil manufacturing company manufactures around 140 units of utensils. Depending upon the availability of row material and other conditions the daily production has been varying from 136 units of utensils to 144 units of utensils whose probability is asiven below.
$\begin{array}{lllllllllll}\text { Production } & 1364 & 137 & 138 & 139 & 140 & 141 & 142 & 143 & 144\end{array}$ per day
$\begin{array}{lllllllll}\text { Probability } & 0.09 .03 & 0.06 & 0.14 & 0.13 & 0.22 & 0.16 & 0.12 & 0.08 \\ 0.06\end{array}$
The finishe units of utensils are transported in a specially designed rickshaw that cargaccommodate only 140 units of utensils. Using the following given randoni numbers simulate the process to find out (1) What will be the average number of utensils waiting in the factory? (2) What will be the number of empty spaces in rickshaw
Random Numbers: 84, 72, 28, 52, 38, 65, 13, 79, 27, 54, 01
(b) Solve the cargo loading problem with following data and maximum weight capacity is five.

| Item (n) | Weight <br> $(\mathrm{Wn})$ | Return <br> $(\mathrm{Rn})$ |
| :---: | :---: | :---: |
| 1 | 1 | 3 |
| 2 | 2 | 7 |
| 3 | 3 | 10 |

Q. 5 (a) Explain the following terms in connection with inventory management. (1) Reorder point (2) Safety stock (3) Lead time (4) Economic lot size (5) Carrying cost
(b) Explain the term crashing of network. Why it is required?

## OR

Q. 5 (a) The annual demand of a product is 15,000 units. Each unit cost Rs.50/- if the orders are placed in quantity below 150 units. For order of 200 and above the unit prize is Rs.44/-. Assume inventory holding cost is $12 \%$ of the value of item and ordering cost is Rs.2/- per order find the economic lot size
(b) A company is presently buying an item of worth Rs. $90,000 /$ - from a supplier at an optimal purchasing policy at a discount of $1 \%$. Presently the ordering cost is Rs.100/- per order and $20 \%$ as inventory handling cost of the average inventory level. The company receives another two offers from the other suppliers. First supplier offers $5 \%$ discount if the order is placed twice a year and second supplier offers $3 \%$ discount if the order is placed quarterly a year. Which offer the company should accept?

